Implementing Multiparty Computation

A VIFF Case Study http://viff.dk/

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Outline

Overview

Multiparty Computation Virtual Ideal Functionality Framework

Design

Network Environment Asynchronicity Program Counters

Conclusion

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Quick Recap of Multiparty Computation



- n players
- wish to jointly compute f
- player P_i has input x_i
- players learn $y = f(x_1, x_2, \dots, x_n)$

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- player P_i has input x_i
- players learn $y = f(x_1, x_2, \dots, x_n)$
- up to t players are corrupt
- must keep inputs private
- must ensure correct output
- players only learn y

Requirements

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- fast cryptosystems
- fast hash functions
- and so on...

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- fast hash functions
- and so on...

But we also need:

- fast cryptographic protocols
- flexible protocol description language
- efficient usage of network resources

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i = int(sys.argv[1]) $(a, b, c) = shamir_share(i)$ x = a * b + cprint open(x) # read commandline argument
 # Shamir secret share input
 # secure multiparty computation
 # broadcast and recombine

(we almost got there)

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- we wanted to write:

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print open(x)	<i># broadcast and recombine</i>

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we also wanted this code to execute in one round:

 $\begin{aligned} \mathbf{x} &= \mathbf{a} \, \ast \, \mathbf{b} \\ \mathbf{y} &= \mathbf{b} \, \ast \, \mathbf{c} \\ \mathbf{z} &= \mathbf{c} \, \ast \, \mathbf{a} \end{aligned}$

we wanted to do MPC over real networks, i.e., the Internet

Applications

We have implemented a number of applications in VIFF:

- Distributed AES
- Distributed RSA
- Double Auction
- Voting
- Poker

Related Projects

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Sharemind — http://sharemind.cs.ut.ee/

- computation over the ring $\mathbb{Z}_{2^{32}}$
- C++ implementation
- scalable to very large data sets
- own MPC assembler language and compiler

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Asynchronous vs. Synchronous Network

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- all rounds equally fast
- optimal execution

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Transport Protocol

We currently use SSL over TCP:

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UDP would be an interesting alternative:

- discrete packets send one share per packet
- we do not care about reordering
- most protocols can handle some dropped packets!

Network Architecture

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SIMAP used a central coordinator:

- forwards packets only
- makes NAT-traversal simple
- a potential bottle-neck

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a.add(b).sub(a.mul(b).mul(2))

$$\Rightarrow$$
 a + b - 2 * a * b

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$$a + b - 2 * a * b$$

- absolutely everything is interpreted
- lack of static types enables stupid mistakes

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- provides full access to Python standard library
- however, we cannot use control structures directly:

if rt.open(a < b and b < c):
 print "Wow, monotone!"</pre>

Must rewrite as:

```
def check_monotone(result):
    if result:
        print "Wow, monotone!"
    x = rt.open(a < b and b < c)
    x.addCallback(check_monotone)</pre>
```

Iong-term solution: put a DSL on top of VIFF

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Asynchronous communication via callbacks:

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- this can lead to an unnatural way of programming
- completely single-threaded no blocking the event loop!

More on Deferreds

We use Deferreds heavily:

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- adding a callback costs at least 300 bytes more
- it is easy to allocate lots of Deferreds:

```
for i in range(10000):
x = x * x
```

all 10,000 multiplications are scheduled immediately:

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Threads are the main alternative to callbacks:

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- can use multiple cores!
- normal program flow, you can block when you want
- thread-switches supposedly have some overhead
- must synchronize threads (and avoid dead-locks...)
- need a way to specify future tasks (callbacks...)

Network delay kills throughput unless we run things in parallel:

▶ like a CPU, we pipeline many operations in parallel

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- can potentially remove idle time:



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Automatic pipelining

VIFF will automatically pipeline everything:

- network traffic begins upon return to event loop
- no notion of rounds
- fits naturally with asynchronous execution

Why We Must Keep Track of Things

Consider this very high-level code for multiplication:

```
def mul(share_a, share_b):
    result = gather_shares([share_a, share_b])
    result.addCallback(finish_mul)
    return result
```

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We now have a problem:

- finish_mul is executed when a and b arrives
- finish_mul is executed when c and d arrives
- other players cannot know which pair arrives first!

Program Counters

VIFF use program counters to track operations:



Program Counter Properties

- assignment depends on program structure
- ensures deterministic assignments
- unique labels for each operation

Preprocessing

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- ► an off-line phase which is independent of actual input
- ► an on-line phase which do depend on the input
- A good example is an actively secure multiplication:
 - ▶ generate a random triple ([*a*], [*b*], [*ab*]) off-line
 - use it to multiply [x] and [y]:

$$d = \operatorname{open}([x] - [a])$$
$$e = \operatorname{open}([y] - [b])$$
$$[xy] = de + d[y] + e[x] + [ab]$$

But how to implement this?

Program Counters Strikes Again!

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Will the program always use the same program counters?

▶ yes! — otherwise it would leak information on the inputs

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